



Summer 2015 Examination

Subject & Code: Basic Maths (17104)

Model Answer

Page No: 1/32

Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
		<p>Important Instructions to the Examiners:</p> <ol style="list-style-type: none">1) The Answers should be examined by key words and not as word-to-word as given in the model answer scheme.2) The model answer and the answer written by candidate may vary but the examiner may try to assess the understanding level of the candidate.3) The language errors such as grammatical, spelling errors should not be given more importance. (Not applicable for subject English and Communication Skills.)4) While assessing figures, examiner may give credit for principal components indicated in the figure. The figures drawn by the candidate and those in the model answer may vary. The examiner may give credit for any equivalent figure drawn.5) Credits may be given step wise for numerical problems. In some cases, the assumed constant values may vary and there may be some difference in the candidate's Answers and the model answer.6) In case of some questions credit may be given by judgment on part of examiner of relevant answer based on candidate's understanding.7) For programming language papers, credit may be given to any other program based on equivalent concept. <p>-----</p> <p>-----</p> <p style="text-align: center;">Important Note</p> <p>In the solution of the question paper, wherever possible all the possible alternative methods of solution are given for the sake of convenience. Still student may follow a method other than the given herein. In such case, FIRST SEE whether the method falls within the scope of the curriculum, and THEN ONLY give appropriate marks in accordance with the scheme of marking.</p> <p>-----</p> <p>-----</p>		



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
1)		Attempt any TEN of the following:		
	a)	Find x , if $\begin{vmatrix} 4 & 3 & 9 \\ 3 & -2 & 7 \\ 11 & 4 & x \end{vmatrix} = 0$.		
	Ans.	$\therefore 4(-2x-28)-3(3x-77)+9(12+22)=0$ $\therefore -8x-112-9x+231+306=0$ $\therefore -17x+425=0$ $\therefore x = \frac{425}{17}$ $\therefore \boxed{x = 25}$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$	2
b)	Prove that the matrix $\begin{bmatrix} 1 & 4 \\ 6 & 9 \end{bmatrix}$ is a nonsingular matrix.			
Ans.	$\therefore \begin{vmatrix} 1 & 4 \\ 6 & 9 \end{vmatrix} = 9-24$ $= -15$ $\neq 0$ Given matrix is non-singular.	1 $\frac{1}{2}$ $\frac{1}{2}$	2	
c)	If $A = \begin{bmatrix} 3 & 4 & -2 \\ 2 & 1 & 0 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & -1 \\ 3 & 4 \\ 0 & 2 \end{bmatrix}$, find AB .			
Ans.	$\therefore AB = \begin{bmatrix} 3 & 4 & -2 \\ 2 & 1 & 0 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ 3 & 4 \\ 0 & 2 \end{bmatrix}$ $= \begin{bmatrix} 6+12-0 & -3+16-4 \\ 4+3+0 & -2+4+0 \end{bmatrix}$ $= \begin{bmatrix} 18 & 9 \\ 7 & 2 \end{bmatrix}$	1 1	2	



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
1)	d)	Resolve into partial fractions $\frac{1}{x^3 - x}$.		
	Ans.	$\frac{1}{x^3 - x} = \frac{1}{x(x+1)(x-1)}$ $= \frac{A}{x} + \frac{B}{x+1} + \frac{C}{x-1}$ $\therefore 1 = (x+1)(x-1)A + x(x-1)B + x(x+1)C$ <p>Put $x = 0$</p> $\therefore 1 = (0+1)(0-1)A + 0 + 0$ $\therefore 1 = -A$ $\therefore \boxed{-1 = A}$ <p>Put $x = -1$</p> $\therefore 1 = 0 - 1(-1-1)B + 0$ $\therefore 1 = 2B$ $\therefore \boxed{\frac{1}{2} = B}$ <p>Put $x = 1$</p> $\therefore 1 = 0 + 0 + 1(1+1)C$ $\therefore 1 = 2C$ $\therefore \boxed{\frac{1}{2} = C}$ $\therefore \frac{1}{x^3 - x} = \frac{-1}{x} + \frac{1}{2(x+1)} + \frac{1}{2(x-1)}$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$	2
	e)	Define compound angle.		
	Ans.	Compound Angle: An angle formed by sum or difference of many angles is said to be compound angle. Note: The above definition is a sample format. Students may express the same into other words also. Please give due credit to the students.	2	2



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
1)	f)	Prove that $\sin\left(\frac{\pi}{2} + \theta\right) = \cos \theta$		
	Ans.	$\begin{aligned}\sin\left(\frac{\pi}{2} + \theta\right) &= \sin \frac{\pi}{2} \cos \theta + \cos \frac{\pi}{2} \sin \theta \\ &= \cos \theta + 0 \\ &= \cos \theta\end{aligned}$	$\frac{1}{2}$ 1 $\frac{1}{2}$	2
	g)	Express $4 \cos 30^\circ \sin 20^\circ$ as the sum or difference of trigonometric ratios.		
Ans.	$\begin{aligned}4 \cos 30^\circ \sin 20^\circ &= 2(2 \cos 30^\circ \sin 20^\circ) \\ &= 2[\sin(30^\circ + 20^\circ) - \sin(30^\circ - 20^\circ)] \\ &= 2[\sin 50^\circ - \sin 10^\circ]\end{aligned}$	1 1	2	
h)	Find the principal value of $\cos\left[\frac{\pi}{2} - \sin^{-1}\left(\frac{1}{2}\right)\right]$			
Ans.	$\begin{aligned}\cos\left[\frac{\pi}{2} - \sin^{-1}\left(\frac{1}{2}\right)\right] &= \cos\left[\frac{\pi}{2} - \frac{\pi}{6}\right] \\ &= \cos\left[\frac{\pi}{3}\right] \\ &= \frac{1}{2} \text{ or } 0.5\end{aligned}$	$\frac{1}{2}$ $\frac{1}{2}$ 1	2	
		OR		
		$\begin{aligned}\cos\left[\frac{\pi}{2} - \sin^{-1}\left(\frac{1}{2}\right)\right] &= \cos[90^\circ - 30^\circ] \\ &= \cos[60^\circ] \\ &= \frac{1}{2} \text{ or } 0.5\end{aligned}$	$\frac{1}{2}$ $\frac{1}{2}$ 1	2
		OR		
		$\begin{aligned}\sin^{-1}\left(\frac{1}{2}\right) &= \frac{\pi}{6} \\ \therefore \cos\left[\frac{\pi}{2} - \sin^{-1}\left(\frac{1}{2}\right)\right] &= \cos\left[\frac{\pi}{2} - \frac{\pi}{6}\right] \\ &= \cos\left[\frac{\pi}{3}\right] \\ &= \frac{1}{2} \text{ or } 0.5\end{aligned}$	$\frac{1}{2}$ $\frac{1}{2}$ 1	2



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks												
1)	i)	Show that the lines $5x+6y-1=0$ and $6x-5y+3=0$ are perpendicular.														
	Ans.	<p>i) For the line $5x+6y-1=0$ $\therefore \text{slope } m_1 = -\frac{A}{B} = -\frac{5}{6}$</p> <p>ii) For the line $6x-5y+3=0$ $\therefore \text{slope } m_2 = -\frac{A}{B} = -\frac{6}{-5} = \frac{6}{5}$ $\therefore m_1 = -\frac{5}{6} = -\frac{1}{6/5} = -\frac{1}{m_2}$ \therefore the lines are perpendicular.</p> <p style="text-align: center;">OR</p> <p>$\therefore m_1 \cdot m_2 = -\frac{5}{6} \times \frac{6}{5} = -1$ \therefore the lines are perpendicular.</p> <p>-----</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>OR</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>	<p>2</p> <p>2</p>												
	j)	Find the equation of straight line passing through $(4, -5)$ and having slope $-\frac{2}{3}$.														
Ans.	<p>\therefore the equation is $y - y_1 = m(x - x_1)$ $\therefore y + 5 = -\frac{2}{3}(x - 4)$ $\therefore 3y + 15 = -2x + 8$ $\therefore 2x + 3y + 7 = 0$</p> <p>-----</p>	<p>1</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>	<p>2</p>													
k)	Find the range and coefficient of range of the following distribution:															
		<table border="1"><tr><td>x_i</td><td>10</td><td>20</td><td>30</td><td>40</td><td>50</td></tr><tr><td>f_i</td><td>7</td><td>5</td><td>3</td><td>2</td><td>1</td></tr></table>	x_i	10	20	30	40	50	f_i	7	5	3	2	1		
x_i	10	20	30	40	50											
f_i	7	5	3	2	1											



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
1)	Ans.	$\begin{aligned} \text{Range} &= \text{Largest Value} - \text{Smallest Value} \\ &= 50 - 10 \\ &= 40 \end{aligned}$ $\begin{aligned} \text{Coefficient of Range} &= \frac{\text{Largest Value} - \text{Smallest Value}}{\text{Largest Value} + \text{Smallest Value}} \\ &= \frac{50 - 10}{50 + 10} \\ &= \frac{2}{3} \end{aligned}$ <hr/>	$\frac{1}{2}$ $\frac{1}{2}$	2
	l)	If the mean is 82.5, standard deviation is 7.2, find the coefficient of variance.		
	Ans.	$\begin{aligned} \text{Coeff. of Variance} &= \frac{S.D.}{\bar{x}} \times 100 \\ &= \frac{7.2}{82.5} \times 100 \\ &= 8.727 \end{aligned}$ <hr/>	1 1	2
2)		Attempt any four of the following:		
	a)	Solve the following equations by using Cramer's rule: $x + y = 4 - z$, $y + z = 1 - 2x$, $x + z = y$		
	Ans.	$\begin{aligned} x + y + z &= 4 \\ 2x + y + z &= 1 \\ x - y + z &= 0 \end{aligned}$ $D = \begin{vmatrix} 1 & 1 & 1 \\ 2 & 1 & 1 \\ 1 & -1 & 1 \end{vmatrix} = 1(1+1) - 1(2-1) + 1(-2-1)$ $= -2$ $D_x = \begin{vmatrix} 4 & 1 & 1 \\ 1 & 1 & 1 \\ 0 & -1 & 1 \end{vmatrix} = 4(1+1) - 1(1-0) + 1(-1-0)$ $= 6$	1 $\frac{1}{2}$	



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
2)		$D_y = \begin{vmatrix} 1 & 4 & 1 \\ 2 & 1 & 1 \\ 1 & 0 & 1 \end{vmatrix} = 1(1-0) - 4(2-1) + 1(0-1)$ $= -4$ $D_z = \begin{vmatrix} 1 & 1 & 4 \\ 2 & 1 & 1 \\ 1 & -1 & 0 \end{vmatrix} = 1(0+1) - 1(0-1) + 4(-2-1)$ $= -10$ $\therefore x = \frac{D_x}{D} = \frac{6}{-2} = -3$ $y = \frac{D_y}{D} = \frac{-4}{-2} = 2$ $z = \frac{D_z}{D} = \frac{-10}{-2} = 5$	<p>1/2</p> <p>1/2</p> <p>1/2</p> <p>1/2</p>	4
	b)	Find the matrix X such that $\begin{bmatrix} 4 & 5 \\ -3 & 6 \end{bmatrix} + X = \begin{bmatrix} 10 & -1 \\ 0 & -6 \end{bmatrix}$		
	Ans.	$\therefore X = \begin{bmatrix} 10 & -1 \\ 0 & -6 \end{bmatrix} - \begin{bmatrix} 4 & 5 \\ -3 & 6 \end{bmatrix}$ $= \begin{bmatrix} 10-4 & -1-5 \\ 0+3 & -6-6 \end{bmatrix}$ $= \begin{bmatrix} 6 & -6 \\ 3 & -12 \end{bmatrix}$	<p>1</p> <p>1</p> <p>2</p>	4
		OR		
		<p>Let $X = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$</p> $\therefore \begin{bmatrix} 4 & 5 \\ -3 & 6 \end{bmatrix} + \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} 10 & -1 \\ 0 & -6 \end{bmatrix}$ $\therefore \begin{bmatrix} 4+a & 5+b \\ -3+c & 6+d \end{bmatrix} = \begin{bmatrix} 10 & -1 \\ 0 & -6 \end{bmatrix}$ $\therefore 4+a=10 \quad 5+b=-1$ $-3+c=0 \quad 6+d=-6$ $\therefore a=6 \quad b=-6$ $c=3 \quad d=-12$ $\therefore X = \begin{bmatrix} 6 & -6 \\ 3 & -12 \end{bmatrix}$	<p>1</p> <p>1</p> <p>1</p> <p>1</p>	4



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
2)	c)	If $A = \begin{bmatrix} 1 & -2 \\ -3 & -1 \end{bmatrix}$, $B = \begin{bmatrix} 4 & 2 & -5 \\ 1 & 0 & 3 \end{bmatrix}$, $C = \begin{bmatrix} 6 & -7 & 0 \\ -1 & 2 & 5 \\ 1 & 0 & 3 \end{bmatrix}$, prove that $(AB)C = A(BC)$		
	Ans.	$A = \begin{bmatrix} 1 & -2 \\ -3 & -1 \end{bmatrix}$, $B = \begin{bmatrix} 4 & 2 & -5 \\ 1 & 0 & 3 \end{bmatrix}$, $C = \begin{bmatrix} 6 & -7 & 0 \\ -1 & 2 & 5 \\ 1 & 0 & 3 \end{bmatrix}$ $AB = \begin{bmatrix} 1 & -2 \\ -3 & -1 \end{bmatrix} \begin{bmatrix} 4 & 2 & -5 \\ 1 & 0 & 3 \end{bmatrix}$ $= \begin{bmatrix} 4-2 & 2-0 & -5-6 \\ -12-1 & -6-0 & 15-3 \end{bmatrix}$ $= \begin{bmatrix} 2 & 2 & -11 \\ -13 & -6 & 12 \end{bmatrix}$ $(AB)C = \begin{bmatrix} 2 & 2 & -11 \\ -13 & -6 & 12 \end{bmatrix} \begin{bmatrix} 6 & -7 & 0 \\ -1 & 2 & 5 \\ 1 & 0 & 3 \end{bmatrix}$ $= \begin{bmatrix} 12-2-11 & -14+4-0 & 0+10-33 \\ -78+6+12 & 91-12+0 & 0-30+36 \end{bmatrix}$ $= \begin{bmatrix} -1 & -10 & -23 \\ -60 & 79 & 6 \end{bmatrix}$ $BC = \begin{bmatrix} 4 & 2 & -5 \\ 1 & 0 & 3 \end{bmatrix} \begin{bmatrix} 6 & -7 & 0 \\ -1 & 2 & 5 \\ 1 & 0 & 3 \end{bmatrix}$ $= \begin{bmatrix} 24-2-5 & -28+4-0 & 0+10-15 \\ 6-0+3 & -7+0+0 & 0+0+9 \end{bmatrix}$ $= \begin{bmatrix} 17 & -24 & -5 \\ 9 & -7 & 9 \end{bmatrix}$ $A(BC) = \begin{bmatrix} 1 & -2 \\ -3 & -1 \end{bmatrix} \begin{bmatrix} 17 & -24 & -5 \\ 9 & -7 & 9 \end{bmatrix}$ $= \begin{bmatrix} 17-18 & -24+14 & -5-18 \\ -51-9 & 72+7 & 15-9 \end{bmatrix}$ $= \begin{bmatrix} -1 & -10 & -23 \\ -60 & 79 & 6 \end{bmatrix}$ $\therefore (AB)C = A(BC)$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$	
		OR		4



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
2)		$(AB)C = \left\{ \begin{bmatrix} 1 & -2 \\ -3 & -1 \end{bmatrix} \begin{bmatrix} 4 & 2 & -5 \\ 1 & 0 & 3 \end{bmatrix} \right\} \begin{bmatrix} 6 & -7 & 0 \\ -1 & 2 & 5 \\ 1 & 0 & 3 \end{bmatrix}$ $= \left\{ \begin{bmatrix} 4-2 & 2-0 & -5-6 \\ -12-1 & -6-0 & 15-3 \end{bmatrix} \right\} \begin{bmatrix} 6 & -7 & 0 \\ -1 & 2 & 5 \\ 1 & 0 & 3 \end{bmatrix}$ $= \begin{bmatrix} 2 & 2 & -11 \\ -13 & -6 & 12 \end{bmatrix} \begin{bmatrix} 6 & -7 & 0 \\ -1 & 2 & 5 \\ 1 & 0 & 3 \end{bmatrix}$ $= \begin{bmatrix} 12-2-11 & -14+4-0 & 0+10-33 \\ -78+6+12 & 91-12+0 & 0-30+36 \end{bmatrix}$ $= \begin{bmatrix} -1 & -10 & -23 \\ -60 & 79 & 6 \end{bmatrix}$ $A(BC) = \begin{bmatrix} 1 & -2 \\ -3 & -1 \end{bmatrix} \left\{ \begin{bmatrix} 4 & 2 & -5 \\ 1 & 0 & 3 \end{bmatrix} \begin{bmatrix} 6 & -7 & 0 \\ -1 & 2 & 5 \\ 1 & 0 & 3 \end{bmatrix} \right\}$ $= \begin{bmatrix} 1 & -2 \\ -3 & -1 \end{bmatrix} \left\{ \begin{bmatrix} 24-2-5 & -28+4-0 & 0+10-15 \\ 6-0+3 & -7+0+0 & 0+0+9 \end{bmatrix} \right\}$ $= \begin{bmatrix} 1 & -2 \\ -3 & -1 \end{bmatrix} \begin{bmatrix} 17 & -24 & -5 \\ 9 & -7 & 9 \end{bmatrix}$ $= \begin{bmatrix} 17-18 & -24+14 & -5-18 \\ -51-9 & 72+7 & 15-9 \end{bmatrix}$ $= \begin{bmatrix} -1 & -10 & -23 \\ -60 & 79 & 6 \end{bmatrix}$ <p>$\therefore (AB)C = A(BC)$</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>	4
	d)	<p>Express the matrix A as sum of symmetric and skew-symmetric matrices, if $A = \begin{bmatrix} -1 & 7 & 1 \\ 2 & 3 & 4 \\ 5 & 0 & 5 \end{bmatrix}$</p>		
	Ans.	<p>$\therefore A' = \begin{bmatrix} -1 & 2 & 5 \\ 7 & 3 & 0 \\ 1 & 4 & 5 \end{bmatrix}$</p>	1	



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
2)		$\therefore A + A' = \begin{bmatrix} -1 & 7 & 1 \\ 2 & 3 & 4 \\ 5 & 0 & 5 \end{bmatrix} + \begin{bmatrix} -1 & 2 & 5 \\ 7 & 3 & 0 \\ 1 & 4 & 5 \end{bmatrix}$ $= \begin{bmatrix} -2 & 9 & 6 \\ 9 & 6 & 4 \\ 6 & 4 & 10 \end{bmatrix}$ $\therefore A - A' = \begin{bmatrix} -1 & 7 & 1 \\ 2 & 3 & 4 \\ 5 & 0 & 5 \end{bmatrix} - \begin{bmatrix} -1 & 2 & 5 \\ 7 & 3 & 0 \\ 1 & 4 & 5 \end{bmatrix}$ $= \begin{bmatrix} 0 & 5 & -4 \\ -5 & 0 & 4 \\ 4 & -4 & 0 \end{bmatrix}$ $\therefore A = \frac{1}{2}(A + A') + \frac{1}{2}(A - A')$ $= \frac{1}{2} \begin{bmatrix} -2 & 9 & 6 \\ 9 & 6 & 4 \\ 6 & 4 & 10 \end{bmatrix} + \frac{1}{2} \begin{bmatrix} 0 & 5 & -4 \\ -5 & 0 & 4 \\ 4 & -4 & 0 \end{bmatrix}$ <p style="text-align: center;">OR</p> $\therefore A = \frac{1}{2}(A + A') + \frac{1}{2}(A - A')$ $= \frac{1}{2} \left\{ \begin{bmatrix} -1 & 7 & 1 \\ 2 & 3 & 4 \\ 5 & 0 & 5 \end{bmatrix} + \begin{bmatrix} -1 & 2 & 5 \\ 7 & 3 & 0 \\ 1 & 4 & 5 \end{bmatrix} \right\} + \frac{1}{2} \left\{ \begin{bmatrix} -1 & 7 & 1 \\ 2 & 3 & 4 \\ 5 & 0 & 5 \end{bmatrix} - \begin{bmatrix} -1 & 2 & 5 \\ 7 & 3 & 0 \\ 1 & 4 & 5 \end{bmatrix} \right\}$ $= \frac{1}{2} \begin{bmatrix} -2 & 9 & 6 \\ 9 & 6 & 4 \\ 6 & 4 & 10 \end{bmatrix} + \frac{1}{2} \begin{bmatrix} 0 & 5 & -4 \\ -5 & 0 & 4 \\ 4 & -4 & 0 \end{bmatrix}$	1 1 1	4
	e)	Resolve into partial fractions $\frac{x+5}{x^2-x}$		
	Ans.	$\frac{x+5}{x^2-x} = \frac{x+5}{x(x-1)} = \frac{A}{x} + \frac{B}{x-1}$ $\therefore \boxed{x+5 = (x-1)A + xB}$	1	4



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
2)		<p>Put $x = 0$ $\therefore 0 + 5 = (0 - 1)A + 0$ $\therefore 5 = -A$ $\therefore \boxed{-5 = A}$</p> <p>Put $x - 1 = 0 \quad \therefore x = 1$ $\therefore 1 + 5 = 0A + B$ $\therefore \boxed{6 = B}$</p> $\therefore \boxed{\frac{x+5}{x^2-x} = \frac{-5}{x} + \frac{6}{x-1}}$	1 1 1	4
		<p>Note for partial fraction problems: The problems of partial fractions could also be solved by the method of "equating equal power coefficients". This method is also applicable. Give appropriate marks in accordance with the scheme of marking in the later/previous problems as the solution by this method is not discussed. For the sake of convenience, the solution of the above problem with the help of this method is illustrated hereunder.</p>		
		$\frac{x+5}{x^2-x} = \frac{x+5}{x(x-1)} = \frac{A}{x} + \frac{B}{x-1}$ $\therefore x+5 = (x-1)A + xB$ $\therefore x+5 = xA - A + xB$ $\therefore 1 \cdot x + 5 = (A+B)x - A$ $\therefore A+B = 1, \quad -A = 5$ $\therefore \boxed{A = -5}$ $\therefore B = 1 - A = 1 + 5$ $\therefore \boxed{B = 6}$ $\therefore \boxed{\frac{1}{x^2-x} = \frac{-5}{x} + \frac{6}{x-1}}$	1 1 1 1	4
		<p>Note: The above problem can also be solved as follows:</p> $\frac{x+1}{x^2-x} = \frac{x+1}{(x-1)x} = \frac{A}{x-1} + \frac{B}{x}$ <p>In this case, we get</p> $\therefore \boxed{A = 6} \quad \boxed{B = -5}$ $\therefore \boxed{\frac{x+1}{x^2-x} = \frac{6}{x-1} + \frac{-5}{x}}$		



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
3)		<p>Attempt any four of the following:</p> <p>a)</p> <p>Find the inverse of the matrix $\begin{bmatrix} 1 & 2 & 4 \\ -1 & 2 & 3 \\ 1 & 4 & 1 \end{bmatrix}$</p> <p>Ans.</p> <p>Let $A = \begin{bmatrix} 1 & 2 & 4 \\ -1 & 2 & 3 \\ 1 & 4 & 1 \end{bmatrix}$</p> <p>$\therefore A = 1(2-12) - 2(-1-3) + 4(-4-2) = -26$</p> <p>$\therefore A^{-1}$ exists.</p> <p>Matrix of Cofactor of A is,</p> $C(A) = \begin{bmatrix} \begin{vmatrix} 2 & 3 \\ 4 & 1 \end{vmatrix} & -\begin{vmatrix} -1 & 3 \\ 1 & 1 \end{vmatrix} & \begin{vmatrix} -1 & 2 \\ 1 & 4 \end{vmatrix} \\ -\begin{vmatrix} 2 & 4 \\ 4 & 1 \end{vmatrix} & \begin{vmatrix} 1 & 4 \\ 1 & 1 \end{vmatrix} & -\begin{vmatrix} 1 & 2 \\ 1 & 4 \end{vmatrix} \\ \begin{vmatrix} 2 & 4 \\ 2 & 3 \end{vmatrix} & -\begin{vmatrix} 1 & 4 \\ -1 & 3 \end{vmatrix} & \begin{vmatrix} 1 & 2 \\ -1 & 2 \end{vmatrix} \end{bmatrix}$ <p>$= \begin{bmatrix} -10 & 4 & -6 \\ 14 & -3 & -2 \\ -2 & -7 & 4 \end{bmatrix}$ ---(*)</p> <p>$adj(A) = \begin{bmatrix} -10 & 14 & -2 \\ 4 & -3 & -7 \\ -6 & -2 & 4 \end{bmatrix}$</p> <p>$\therefore A^{-1} = \frac{1}{ A } adj(A)$</p> $= \frac{1}{-26} \begin{bmatrix} -10 & 14 & -2 \\ 4 & -3 & -7 \\ -6 & -2 & 4 \end{bmatrix}$	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$1\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>1</p>	<p>4</p>
		<p>(*) Note: In the matrix $C(A)$, if 1 to 3 elements are wrong (either in sign or value), deduct $\frac{1}{2}$ mark, if 4 to 6 elements are wrong, deduct $1\frac{1}{2}$ marks, if 7 to 9 are wrong, deduct all the 2 marks. Further, if all the elements in the last i.e., $adj(A)$ are correct, then only give $\frac{1}{2}$ mark.</p> <p style="text-align: center;">OR</p>	OR	



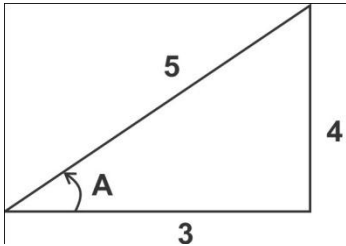
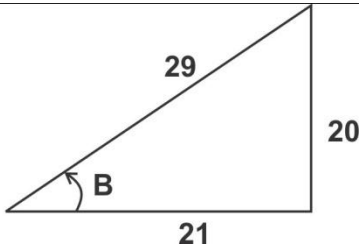
Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
3)		<p>Matrix of minors of A is,</p> $M(A) = \begin{bmatrix} \begin{vmatrix} 2 & 3 \\ 4 & 1 \end{vmatrix} & \begin{vmatrix} -1 & 3 \\ 1 & 1 \end{vmatrix} & \begin{vmatrix} -1 & 2 \\ 1 & 4 \end{vmatrix} \\ \begin{vmatrix} 2 & 4 \\ 4 & 1 \end{vmatrix} & \begin{vmatrix} 1 & 4 \\ 1 & 1 \end{vmatrix} & \begin{vmatrix} 1 & 2 \\ 1 & 4 \end{vmatrix} \\ \begin{vmatrix} 2 & 4 \\ 2 & 3 \end{vmatrix} & \begin{vmatrix} 1 & 4 \\ -1 & 3 \end{vmatrix} & \begin{vmatrix} 1 & 2 \\ -1 & 2 \end{vmatrix} \end{bmatrix}$ $= \begin{bmatrix} -10 & -4 & -6 \\ -14 & -3 & 2 \\ -2 & 7 & 4 \end{bmatrix} \quad \text{---(*)}$ $C(A) = \begin{bmatrix} -10 & 4 & -6 \\ 14 & -3 & -2 \\ -2 & -7 & 4 \end{bmatrix}$ <p style="text-align: center;">OR</p> $A_{11} = \begin{vmatrix} 2 & 3 \\ 4 & 1 \end{vmatrix} = -10 \quad A_{12} = -\begin{vmatrix} -1 & 3 \\ 1 & 1 \end{vmatrix} = 4 \quad A_{13} = \begin{vmatrix} -1 & 2 \\ 1 & 4 \end{vmatrix} = -6$ $A_{21} = -\begin{vmatrix} 2 & 4 \\ 4 & 1 \end{vmatrix} = 14 \quad A_{22} = \begin{vmatrix} 1 & 4 \\ 1 & 1 \end{vmatrix} = -3 \quad A_{23} = -\begin{vmatrix} 1 & 2 \\ 1 & 4 \end{vmatrix} = -2$ $A_{31} = \begin{vmatrix} 2 & 4 \\ 2 & 3 \end{vmatrix} = -2 \quad A_{32} = -\begin{vmatrix} 1 & 4 \\ -1 & 3 \end{vmatrix} = -7 \quad A_{33} = \begin{vmatrix} 1 & 2 \\ -1 & 2 \end{vmatrix} = 4$ $\therefore C(A) = \begin{bmatrix} -10 & 4 & -6 \\ 14 & -3 & -2 \\ -2 & -7 & 4 \end{bmatrix}$ <p>Note: In the above, if 1 to 3 elements are wrong, deduct ½ mark, if 4 to 6 elements are wrong, deduct 1 marks, and if 7 to 9 are wrong, deduct all the marks. Further, if all the elements in the following matrices C(A) and adj (A) are correct, then only give the marks.</p> <p>-----</p>	<p>½</p> <p>1</p> <p>½</p> <p>OR</p> <p>1½</p> <p>½</p>	<p>4</p> <p>4</p>



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
3)	b)	<p>Solve by matrix method: $3x + y + 2z = 3, 2x - 3y - z = -3, x + 2y + z = 4$</p> <p>Ans.</p> $\therefore A = \begin{bmatrix} 3 & 1 & 2 \\ 2 & -3 & -1 \\ 1 & 2 & 1 \end{bmatrix}, X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}, B = \begin{bmatrix} 3 \\ -3 \\ 4 \end{bmatrix}$ $\therefore A = 3(-3+2) - 1(2+1) + 2(4+3) = 8$ $\therefore \text{adj}(A) = \begin{bmatrix} -1 & 3 & 5 \\ -3 & 1 & 7 \\ 7 & -5 & -11 \end{bmatrix} \text{-----} (*)$ $\therefore A^{-1} = \frac{1}{ A } \text{adj}(A)$ $= \frac{1}{8} \begin{bmatrix} -1 & 3 & 5 \\ -3 & 1 & 7 \\ 7 & -5 & -11 \end{bmatrix}$ <p>\therefore the solution is,</p> $X = A^{-1}B$ $= \frac{1}{8} \begin{bmatrix} -1 & 3 & 5 \\ -3 & 1 & 7 \\ 7 & -5 & -11 \end{bmatrix} \begin{bmatrix} 3 \\ -3 \\ 4 \end{bmatrix}$ $= \frac{1}{8} \begin{bmatrix} 8 \\ 16 \\ -8 \end{bmatrix}$ $= \begin{bmatrix} 1 \\ 2 \\ -1 \end{bmatrix}$ <p>$\therefore x = 1, y = 2, z = -1$</p> <p>(*) Note: Many other methods are followed to find $\text{adj}(A)$ as discussed in the Q. 3 (a). Please give appropriate marks in accordance with the scheme of marking as discussed therein.</p>	<p>$\frac{1}{2}$</p> <p>1</p> <p>1</p> <p>1</p> <p>$\frac{1}{2}$</p>	4



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
3)	c)	Resolve into partial fractions $\frac{x^3+1}{x^2+6x}$		
	Ans.	$\frac{x^3+1}{x^2+6x} = x-6 + \frac{36x+1}{x^2+6x}$ $\therefore \frac{36x+1}{x^2+6x} = \frac{36x+1}{x(x+6)} = \frac{A}{x} + \frac{B}{x+6}$ $\therefore \boxed{36x+1 = (x+6)A + xB}$ <p>Put $x=0$</p> $\therefore 0+1 = (0+6)A + 0$ $\therefore 1 = 6A$ $\therefore \boxed{\frac{1}{6} = A}$ <p>Put $x+6=0$ i.e., $x=-6$</p> $\therefore 36(-6)+1 = 0 - 6B$ $\therefore -215 = -6B$ $\therefore \boxed{\frac{215}{6} = B}$ $\therefore \frac{x^3+1}{x^2+6x} = \frac{1}{6} + \frac{215}{6(x+6)}$ $\therefore \boxed{\frac{x^3+1}{x^2+6x} = x-6 + \frac{1}{6} + \frac{215}{6(x+6)}}$	1 1/2 1 1/2 1/2	4
	d)	Resolve into partial fractions $\frac{\tan \theta + 1}{(\tan \theta + 2)(\tan \theta + 3)}$		
	Ans.	<p>Put $\tan \theta = x$</p> $\frac{\tan \theta + 1}{(\tan \theta + 2)(\tan \theta + 3)} = \frac{x+1}{(x+2)(x+3)} = \frac{A}{x+2} + \frac{B}{x+3}$ $\therefore \boxed{x+1 = (x+3)A + (x+2)B}$ <p>Put $x=-2$</p> $\therefore -2+1 = (-2+3)A + 0$ $\therefore \boxed{A = -1}$	1	

Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
3)		<p>Put $x = -3$</p> <p>$\therefore -3 + 1 = 0 + (-3 + 2)B$</p> <p>$\therefore \boxed{B = 2}$</p> <p>$\therefore \frac{x+1}{(x+2)(x+3)} = \frac{-1}{x+2} + \frac{2}{x+3}$</p> <div style="border: 1px solid black; padding: 5px; display: inline-block;"> $\therefore \frac{\tan \theta + 1}{(\tan \theta + 2)(\tan \theta + 3)} = \frac{-1}{\tan \theta + 2} + \frac{2}{\tan \theta + 3}$ </div> <p style="text-align: center;">OR</p> <p>$\frac{\tan \theta + 1}{(\tan \theta + 2)(\tan \theta + 3)} = \frac{A}{\tan \theta + 2} + \frac{B}{\tan \theta + 3}$</p> <p>$\therefore \boxed{\tan \theta + 1 = (\tan \theta + 3)A + (\tan \theta + 2)B}$</p> <p>Put $\tan \theta = -2$</p> <p>$\therefore -2 + 1 = (-2 + 3)A + 0$</p> <p>$\therefore \boxed{A = -1}$</p> <p>Put $\tan \theta = -3$</p> <p>$\therefore -3 + 1 = 0 + (-3 + 2)B$</p> <p>$\therefore \boxed{B = 2}$</p> <div style="border: 1px solid black; padding: 5px; display: inline-block;"> $\therefore \frac{\tan \theta + 1}{(\tan \theta + 2)(\tan \theta + 3)} = \frac{-1}{\tan \theta + 2} + \frac{2}{\tan \theta + 3}$ </div>	<p>1</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>1</p> <p>1</p> <p>1</p>	<p>4</p> <p>4</p>
	e)	<p>If $\cos A = -\frac{3}{5}$, $\sin B = \frac{20}{29}$, where A and B are the angles in the third and second quadrant respectively, find $\tan(A + B)$.</p>		
	Ans.	<div style="display: flex; justify-content: space-around; align-items: flex-end;"> <div style="text-align: center;"> $\cos A = -\frac{3}{5}$  </div> <div style="text-align: center;"> $\sin B = \frac{20}{29}$  </div> </div>		



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
3)		<p>As A is the third quadrant, tan A is positive and B is in the second quadrant, tan B is negative.</p> $\therefore \tan A = \frac{4}{3} \quad \text{and} \quad \tan B = -\frac{20}{21}$ $\therefore \tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$ $= \frac{\frac{4}{3} - \frac{20}{21}}{1 - \left(\frac{4}{3}\right)\left(-\frac{20}{21}\right)} \quad \text{---} (*)$ $= \frac{24}{143} \quad \text{or} \quad 0.168 \quad \text{---} (**)$ <p>Note (*): Due to the use of advance scientific calculators which is permissible in the exam, students may write the step (**) directly after step (*). Writing such step is to be considered.</p> <p>Note: To evaluate value of tan A and tan B, many times the relations between sine ratio and cosine ratio is used (as illustrated hereunder), instead of using Triangle Method as illustrated in the above solution. As the main object is to find the values, please consider these methods also.</p> $\tan A = \frac{\sqrt{1 - \cos^2 A}}{\cos A} = \frac{\sqrt{1 - \frac{9}{25}}}{\frac{3}{5}} = \frac{4}{5}$ $\tan B = -\frac{\sin B}{\sqrt{1 - \sin^2 B}} = -\frac{\frac{20}{29}}{\sqrt{1 - \frac{400}{841}}} = -\frac{20}{21}$ <hr style="border-top: 1px dashed black;"/> <p>f)</p> <p>Without using calculator find the value of $\sin(150^\circ) - \tan(315^\circ) + \cos(300^\circ) + \sec^2(360^\circ)$</p> <p>Ans. $\sin(150^\circ) = \sin(90^\circ + 60^\circ) \quad \text{or} \quad \sin(180^\circ - 30^\circ)$ $= \cos 60^\circ \quad \text{or} \quad \sin 30^\circ$ $= \frac{1}{2}$</p>	<p>1+1</p> <p>1</p> <p>1</p> <p>4</p> <p>1/2</p> <p>1/2</p>	

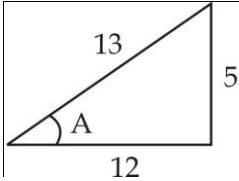
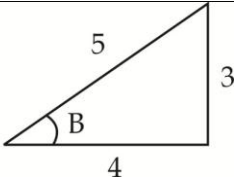


Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
4)		Attempt any four of the following:		
	a)	Prove that $1 + \tan A \cdot \tan 2A = \sec 2A$		
	Ans.	$1 + \tan A \cdot \tan 2A = 1 + \frac{\sin A}{\cos A} \times \frac{\sin 2A}{\cos 2A}$ $= \frac{\cos A \cos 2A + \sin A \sin 2A}{\cos A \cos 2A}$ $= \frac{\cos(A - 2A)}{\cos A \cos 2A}$ $= \frac{\cos(-A)}{\cos A \cos 2A}$ $= \frac{\cos A}{\cos A \cos 2A}$ $= \sec 2A$ <p style="text-align: center;">OR</p> $1 + \tan A \cdot \tan 2A = 1 + \tan A \left(\frac{2 \tan A}{1 - \tan^2 A} \right)$ $= \frac{1 - \tan^2 A + 2 \tan^2 A}{1 - \tan^2 A}$ $= \frac{1 + \tan^2 A}{1 - \tan^2 A}$ $= \sec 2A$	1 1 1 1 1 1 1 1	4 4
	b)	Prove that $\sin(A - B) = \sin A \cos B - \cos A \sin B$		
	Ans.		1	



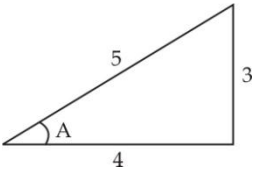
Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
4)		$\begin{aligned} \sin(A-B) &= \frac{NQ}{OQ} \\ &= \frac{RM}{OQ} \\ &= \frac{PM-PR}{OQ} \\ &= \frac{PM}{OQ} - \frac{PR}{OQ} \\ &= \frac{PM}{OP} \times \frac{OP}{OQ} - \frac{PR}{PQ} \times \frac{PQ}{OQ} \\ &= \sin A \cos B - \cos A \sin B \end{aligned}$ <p>Note: The above is proved by different ways in several books. Consider all these proof but check whether the method is falling within the scope of curriculum and give appropriate marks in accordance with the scheme of marking. In accordance with the Teacher's Manual published by MSBTE, the result is treated as Fundamental Result which is not proved by the help of any another result. If the above result is proved by students using any another result, suppose using $\sin(A+B)$, then this result i.e., $\sin(A+B)$ must have been proved first.</p> <p>-----</p> <p>c) If A and B both are obtuse angles and $\sin A = \frac{5}{13}$, $\cos B = -\frac{4}{5}$, find the quadrant of the angle $A+B$.</p> <p>Ans. $\sin A = \frac{5}{13}$, $\cos B = -\frac{4}{5}$ As A and B are obtuse angles, $\cos A$ is negative and $\sin B$ is positive.</p> $\therefore \cos A = -\sqrt{1-\sin^2 A} = -\sqrt{1-\left(\frac{5}{13}\right)^2} = -\frac{12}{13}$ $\sin B = +\sqrt{1-\cos^2 B} = +\sqrt{1-\left(-\frac{4}{5}\right)^2} = \frac{3}{5}$ $\begin{aligned} \therefore \cos(A+B) &= \cos A \cos B - \sin A \sin B \\ &= -\frac{12}{13} \cdot \left(-\frac{4}{5}\right) - \frac{5}{13} \cdot \frac{3}{5} \quad \text{---} (*) \\ &= \frac{33}{65} \quad \text{---} (*) \end{aligned}$	1 1 1	4
			1/2	
			1/2	
			1	
			1	



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
4)		<p>As A and B are obtuse angles, $180^\circ < A + B < 360^\circ$.</p> <p>In III quadrant, \cos is -ve. $\therefore A + B$ is in IV quadrant.</p> <p style="text-align: center;">OR</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;"> $\sin A = \frac{5}{13}$  </div> <div style="text-align: center;"> $\cos B = -\frac{4}{5}$  </div> </div> <p>As A and B are obtuse angles, $\cos A$ is negative and $\sin B$ is positive.</p> <p>$\therefore \cos A = -\frac{12}{13}$</p> <p>$\sin B = \frac{3}{5}$</p> <p>$\therefore \cos(A + B) = \cos A \cos B - \sin A \sin B$</p> $= -\frac{12}{13} \cdot \left(-\frac{4}{5}\right) - \frac{5}{13} \cdot \frac{3}{5} \quad \text{---} (*)$ $= \frac{33}{65} \quad \text{---} (**)$ <p>As A and B are obtuse angles, $180^\circ < A + B < 360^\circ$.</p> <p>In III quadrant, \cos is -ve. $\therefore A + B$ is in IV quadrant.</p> <p style="text-align: center;">OR</p> <p>A and B both are obtuse angles, $\tan A$ and $\tan B$ are negative.</p> <p>$\therefore \tan A = -\frac{5}{12}$ and $\tan B = -\frac{3}{4}$</p> <p>$\therefore \tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$</p> $= \frac{-\frac{5}{12} - \frac{3}{4}}{1 - \left(-\frac{5}{12}\right)\left(-\frac{3}{4}\right)} \quad \text{---} (*)$ $= -\frac{56}{33} \quad \text{or} \quad -1.697 \quad \text{---} (**)$ <p>In the III quadrant \tan is +ve and in the IV quadrant, \tan is -ve. $\therefore A + B$ is in the IV quadrant.</p>	<p style="text-align: center;">1</p> <p style="text-align: center;">$\frac{1}{2}$</p> <p style="text-align: center;">$\frac{1}{2}$</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">$\frac{1}{2} + \frac{1}{2}$</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p>	<p style="text-align: center;">4</p> <p style="text-align: center;">4</p> <p style="text-align: center;">4</p>



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
4)		<p>Note (*): Due to the use of advance scientific calculators which is permissible in the exam, students may write the step (**) directly after step (*). Writing such step is to be considered.</p> <hr/> <p>d) Prove that $\frac{\sin 8x - \sin 5x}{\cos 7x + \cos 6x} = \sin x + \cos x \cdot \tan \frac{x}{2}$</p> <p>Ans. $\frac{\sin 8x - \sin 5x}{\cos 7x + \cos 6x} = \frac{2 \cos \left(\frac{8x+5x}{2} \right) \sin \left(\frac{8x-5x}{2} \right)}{2 \cos \left(\frac{7x+6x}{2} \right) \cos \left(\frac{7x-6x}{2} \right)}$ $= \frac{2 \cos \left(\frac{13x}{2} \right) \sin \left(\frac{3x}{2} \right)}{2 \cos \left(\frac{13x}{2} \right) \cos \left(\frac{x}{2} \right)}$ $= \frac{\sin \left(\frac{3x}{2} \right)}{\cos \left(\frac{x}{2} \right)}$ $= \frac{\sin \left(x + \frac{x}{2} \right)}{\cos \left(\frac{x}{2} \right)}$ $= \frac{\sin x \cos \left(\frac{x}{2} \right) + \cos x \sin \left(\frac{x}{2} \right)}{\cos \left(\frac{x}{2} \right)}$ $= \sin x + \cos x \cdot \tan \frac{x}{2}$ <hr/> <p>e) Prove that $2 \tan^{-1} x = \tan^{-1} \left(\frac{2x}{1-x^2} \right)$</p> <p>Ans. $2 \tan^{-1} x = \tan^{-1} x + \tan^{-1} x$ $= \tan^{-1} \left(\frac{x+x}{1-x.x} \right)$ $= \tan^{-1} \left(\frac{2x}{1-x^2} \right)$</p> </p>	<p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>2</p> <p>1</p>	<p>4</p> <p>4</p>

Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
4)	f)	<p>Prove that $\cos^{-1}\left(\frac{4}{5}\right) + \tan^{-1}\left(\frac{3}{5}\right) = \tan^{-1}\left(\frac{27}{11}\right)$</p> <p>Ans. Let $A = \cos^{-1}\left(\frac{4}{5}\right)$</p> <p>$\therefore \cos A = \frac{4}{5}$</p> <div style="text-align: center;">  </div> <p>$\therefore \tan A = \frac{3}{4}$ ----- (*)</p> <p>$\therefore A = \tan^{-1}\left(\frac{3}{4}\right)$</p> <p>$\therefore \cos^{-1}\left(\frac{4}{5}\right) + \tan^{-1}\left(\frac{3}{5}\right) = \tan^{-1}\left(\frac{3}{4}\right) + \tan^{-1}\left(\frac{3}{5}\right)$</p> $= \tan^{-1}\left(\frac{\frac{3}{4} + \frac{3}{5}}{1 - \frac{3}{4} \cdot \frac{3}{5}}\right)$ $= \tan^{-1}\left(\frac{27}{11}\right)$	<p>1</p> <p>1</p> <p>1</p> <p>1</p>	4
		<p>Note (*): To evaluate value of tan A, various methods are used by students, such as 'using the relation between sin A and tan A' or 'first to find sin A using cos A and find tan A' etc., instead of using Triangle Method as illustrated in the above solution. As main object is to find the value of tan A, please consider these methods also.</p> <hr style="border-top: 1px dashed black;"/>		



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
5)		Attempt any four of the following:		
	a)	Prove that $\frac{\sin 4\theta + \sin 2\theta}{1 + \cos 2\theta + \cos 4\theta} = \tan 2\theta$		
	Ans.	$\frac{\sin 4\theta + \sin 2\theta}{1 + \cos 2\theta + \cos 4\theta} = \frac{\sin 2(2\theta) + \sin 2\theta}{1 + \cos 2(2\theta) + \cos 2\theta}$ $= \frac{2 \sin 2\theta \cos 2\theta + \sin 2\theta}{2 \cos^2 2\theta + \cos 2\theta}$ $= \frac{\sin 2\theta (2 \cos 2\theta + 1)}{\cos 2\theta (2 \cos 2\theta + 1)}$ $= \frac{\sin 2\theta}{\cos 2\theta}$ $= \tan 2\theta$	1 1 1 1	4
	b)	Prove that $\frac{\sin 4A + \sin 5A + \sin 6A}{\cos 4A + \cos 5A + \cos 6A} = \tan 5A$		
	Ans.	$\frac{\sin 4A + \sin 5A + \sin 6A}{\cos 4A + \cos 5A + \cos 6A} = \frac{\sin 4A + \sin 6A + \sin 5A}{\cos 4A + \cos 6A + \cos 5A}$ $= \frac{2 \sin 5A \cos(-A) + \sin 5A}{2 \cos 5A \cos(-A) + \cos 5A}$ $= \frac{\sin 5A [2 \cos(-A) + 1]}{\cos 5A [2 \cos(-A) + 1]}$ $= \tan 5A$	1+1 1 1	4
	c)	Prove that $\tan^{-1} x + \tan^{-1} y = \tan^{-1} \left(\frac{x+y}{1-xy} \right)$, $x > 0$, $y > 0$, $xy < 1$		
	Ans.	<p>Put $\tan^{-1} x = A$ and $\tan^{-1} y = B$</p> <p>$\therefore x = \tan A$ and $y = \tan B$</p> $\therefore \tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$ $= \frac{x+y}{1-xy}$ <p>$\therefore A+B = \tan^{-1} \left(\frac{x+y}{1-xy} \right)$</p> <p>$\therefore \tan^{-1} x + \tan^{-1} y = \tan^{-1} \left(\frac{x+y}{1-xy} \right)$</p>	1 1 1 1	4

Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
5)	d)	Find the angle between the lines $y = 5x + 6$ and $y = x$		
	Ans.	<p>For $y = 5x + 6$ i.e., $5x - y + 6 = 0$ or $-5x + y - 6 = 0$</p> <p>slope $m_1 = -\frac{a}{b} = 5$</p> <p>For $y = x$ or $x - y = 0$,</p> <p>slope $m_2 = -\frac{a}{b} = 1$</p> <p>$\therefore \tan \theta = \left \frac{m_1 - m_2}{1 + m_1 \cdot m_2} \right$</p> <p>$= \left \frac{5 - 1}{1 + (5) \cdot (1)} \right$</p> <p>$= \frac{2}{3}$ or 0.667</p> <p>$\therefore \theta = \tan^{-1} \left(\frac{2}{3} \right)$ or $\tan^{-1}(0.667)$</p>	1	
			1	
			1	
			$\frac{1}{2}$	
			$\frac{1}{2}$	4
	e)	<p>If $P(x_1, y_1)$ is any point and $Ax + By + C = 0$ is a line, prove that the perpendicular distance of a point P from the line is given by $\left \frac{Ax_1 + By_1 + C}{\sqrt{a^2 + b^2}} \right$</p>		
	Ans.	<p>Area of $\Delta PQR = \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ -\frac{C}{A} & 0 & 1 \\ 0 & -\frac{C}{B} & 1 \end{vmatrix}$</p> <p>$= \frac{C}{2AB} (Ax_1 + By_1 + C)$</p> <p>Now $QR = \sqrt{\left(-\frac{C}{A} - 0\right)^2 + \left(0 + \frac{C}{B}\right)^2} = \frac{C\sqrt{A^2 + B^2}}{AB}$</p>	1	
			$\frac{1}{2}$	



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
5)		<p>But Area of $\Delta PQR = \frac{1}{2} \times AB \times PM$</p> $= \frac{1}{2} \times \frac{C\sqrt{A^2+B^2}}{AB} \times p$ $\therefore \frac{1}{2} \times \frac{C\sqrt{A^2+B^2}}{AB} \times p = \frac{C}{2AB} (Ax_1 + By_1 + C)$ $\therefore p = \frac{Ax_1 + By_1 + C}{\sqrt{A^2+B^2}}$ <p>As length is always +ve,</p> $p = \left \frac{Ax_1 + By_1 + C}{\sqrt{A^2+B^2}} \right $	1 1/2 1/2 1/2	4
	f)	<p>Find the equation of line passing through the point of intersection of the lines $2x+3y=13$, $5x-y=7$ and perpendicular to the line $3x-y+7=0$</p>		
	Ans.	$2x+3y=13$ $5x-y=7$ $\therefore 2x+3y=13$ $15x-3y=21$ $\therefore 17x=34$ $\therefore x=2$ $y=3$ <p>\therefore Point of intersection = (2, 3)</p> <p>Slope of the line $3x-y+7=0$ is,</p> $m_0 = -\frac{a}{b} = -\frac{3}{-1} = 3$ <p>\therefore Slope of the required line is,</p> $m = -\frac{1}{m_0} = -\frac{1}{3}$ <p>\therefore equation is,</p> $y - y_1 = m(x - x_1)$ $\therefore y - 3 = -\frac{1}{3}(x - 2)$ $\therefore x + 3y - 11 = 0$	1/2 1/2 1 1 1/2 1/2	4



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
6)		Attempt any four of the following:		
	a)	Find the equation of the lines passing through the point (6, 5) and parallel to the line having intercepts 2 and 4 on X and Y axis respectively.		
	Ans.	<p>slope of given line is $m_0 = -\frac{y-\text{int}}{x-\text{int}} = -\frac{4}{2} = -2$</p> <p style="text-align: center;"><i>OR</i></p> <p>Given line is passing through (2, 0) & (0, 4)</p> <p>\therefore slope of given line is $m_0 = \frac{y_2 - y_1}{x_2 - x_1} = \frac{4-0}{0-2} = -2$</p> <p>$\therefore$ Slope of the required line is,</p> <p style="text-align: center;">$m = m_0 = -2$</p> <p>\therefore equation is,</p> <p style="text-align: center;">$y - y_1 = m(x - x_1)$</p> <p>$\therefore y - 5 = -2(x - 6)$</p> <p>$\therefore y - 5 = -2x + 12$</p> <p>$\therefore 2x + y - 17 = 0$</p> <p>-----</p>	1 or 1 1 1 1	4
	b)	Find the acute angle between the lines $3x - 2y + 4 = 0$ and $2x - 3y - 7 = 0$.		
	Ans.	<p>For $3x - 2y + 4 = 0$,</p> <p>slope $m_1 = -\frac{a}{b} = -\frac{3}{-2} = \frac{3}{2}$</p> <p>For $2x - 3y - 7 = 0$,</p> <p>slope $m_2 = -\frac{a}{b} = -\frac{2}{-3} = \frac{2}{3}$</p> <p>$\therefore \tan \theta = \frac{ m_1 - m_2 }{1 + m_1 \cdot m_2}$</p> <p style="text-align: center;">$= \frac{\left \frac{3}{2} - \frac{2}{3} \right }{1 + \left(\frac{3}{2}\right) \cdot \left(\frac{2}{3}\right)}$</p> <p style="text-align: center;">$= \frac{5}{12} \quad \text{or} \quad 0.417$</p> <p>$\therefore \theta = \tan^{-1}\left(\frac{5}{12}\right) \quad \text{or} \quad \tan^{-1}(0.417) \quad \text{or} \quad 22.636^\circ \quad \text{or} \quad 0.395^c$</p>	$\frac{1}{2}$ $\frac{1}{2}$ 1 1	4



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks																																										
6)		$\therefore \text{Variance} = (S.D.)^2 = 15.7197^2 = 247.109$ $\text{Coeff. of Variance} = \frac{S.D.}{\bar{x}} \times 100$ $= \frac{15.7197}{85.625} \times 100$ $= 18.359$ <p style="text-align: center;">OR</p> $\therefore \text{Variance} = h^2 \left[\frac{\sum f_i d_i^2}{N} - \left(\frac{\sum f_i d_i}{N} \right)^2 \right]$ $= 10^2 \left[\frac{213}{80} - \left(\frac{-35}{80} \right)^2 \right]$ $= 247.109$ $\text{Coeff. of Variance} = \frac{\sqrt{\text{Variance}}}{\bar{x}} \times 100$ $= \frac{\sqrt{247.109}}{82.625} \times 100$ $= 18.359$	<p>1/2</p> <p>1</p> <p>OR</p> <p>1</p> <p>1</p>	<p>4</p> <p>4</p>																																										
	e)	<p>Calculate the standard deviation of the following table:</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>Weekly expenditure Below</td> <td>05</td> <td>10</td> <td>15</td> <td>20</td> <td>25</td> </tr> <tr> <td>No. of Students</td> <td>06</td> <td>16</td> <td>28</td> <td>38</td> <td>46</td> </tr> </table>	Weekly expenditure Below	05	10	15	20	25	No. of Students	06	16	28	38	46																																
Weekly expenditure Below	05	10	15	20	25																																									
No. of Students	06	16	28	38	46																																									
	Ans.	<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>Class</th> <th>xi</th> <th>f_i</th> <th>f_ix_i</th> <th>x_i²</th> <th>f_ix_i²</th> </tr> </thead> <tbody> <tr> <td>0-5</td> <td>2.5</td> <td>6</td> <td>15</td> <td>6.25</td> <td>37.5</td> </tr> <tr> <td>5-10</td> <td>7.5</td> <td>10</td> <td>75</td> <td>56.25</td> <td>562.5</td> </tr> <tr> <td>10-15</td> <td>12.5</td> <td>12</td> <td>150</td> <td>156.25</td> <td>1875</td> </tr> <tr> <td>15-20</td> <td>17.5</td> <td>10</td> <td>175</td> <td>306.25</td> <td>3062.5</td> </tr> <tr> <td>20-25</td> <td>22.5</td> <td>8</td> <td>180</td> <td>506.25</td> <td>4050</td> </tr> <tr> <td></td> <td></td> <td>46</td> <td>595</td> <td></td> <td>9587.5</td> </tr> </tbody> </table> $S.D. = \sqrt{\frac{\sum f_i x_i^2}{N} - \left(\frac{\sum f_i x_i}{N} \right)^2}$ $= \sqrt{\frac{9587.5}{46} - \left(\frac{595}{46} \right)^2}$ $= 6.412$	Class	xi	f _i	f _i x _i	x _i ²	f _i x _i ²	0-5	2.5	6	15	6.25	37.5	5-10	7.5	10	75	56.25	562.5	10-15	12.5	12	150	156.25	1875	15-20	17.5	10	175	306.25	3062.5	20-25	22.5	8	180	506.25	4050			46	595		9587.5	<p>1+1</p> <p>1</p> <p>1</p>	<p>4</p>
Class	xi	f _i	f _i x _i	x _i ²	f _i x _i ²																																									
0-5	2.5	6	15	6.25	37.5																																									
5-10	7.5	10	75	56.25	562.5																																									
10-15	12.5	12	150	156.25	1875																																									
15-20	17.5	10	175	306.25	3062.5																																									
20-25	22.5	8	180	506.25	4050																																									
		46	595		9587.5																																									



Que. No.	Sub. Que.	Model Answers	Marks	Total Marks																																																	
6)		<p>OR</p> <table border="1" style="margin: auto;"> <thead> <tr> <th>Class</th> <th>xi</th> <th>fi</th> <th>di</th> <th>fi di</th> <th>di²</th> <th>fi di²</th> </tr> </thead> <tbody> <tr> <td>0-5</td> <td>2.5</td> <td>6</td> <td>-2</td> <td>-12</td> <td>4</td> <td>24</td> </tr> <tr> <td>5-10</td> <td>7.5</td> <td>10</td> <td>-1</td> <td>-10</td> <td>1</td> <td>10</td> </tr> <tr> <td>10-15</td> <td>12.5</td> <td>12</td> <td>0</td> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>15-20</td> <td>17.5</td> <td>10</td> <td>1</td> <td>10</td> <td>1</td> <td>10</td> </tr> <tr> <td>20-25</td> <td>22.5</td> <td>8</td> <td>2</td> <td>16</td> <td>4</td> <td>32</td> </tr> <tr> <td></td> <td></td> <td>46</td> <td></td> <td>4</td> <td></td> <td>76</td> </tr> </tbody> </table> $S.D. = h \times \sqrt{\frac{\sum f_i d_i^2}{N} - \left(\frac{\sum f_i d_i}{N}\right)^2}$ $= 5 \times \sqrt{\frac{76}{46} - \left(\frac{4}{46}\right)^2}$ $= 6.412$	Class	xi	fi	di	fi di	di ²	fi di ²	0-5	2.5	6	-2	-12	4	24	5-10	7.5	10	-1	-10	1	10	10-15	12.5	12	0	0	0	0	15-20	17.5	10	1	10	1	10	20-25	22.5	8	2	16	4	32			46		4		76	<p>1+1</p> <p>1</p> <p>1</p>	<p>4</p>
Class	xi	fi	di	fi di	di ²	fi di ²																																															
0-5	2.5	6	-2	-12	4	24																																															
5-10	7.5	10	-1	-10	1	10																																															
10-15	12.5	12	0	0	0	0																																															
15-20	17.5	10	1	10	1	10																																															
20-25	22.5	8	2	16	4	32																																															
		46		4		76																																															
	f)	<p>Calculate the mean deviation about the mean of the following distribution:</p> <table border="1" style="margin: auto;"> <thead> <tr> <th>xi</th> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> <td>8</td> </tr> <tr> <th>fi</th> <td>4</td> <td>9</td> <td>10</td> <td>8</td> <td>6</td> <td>3</td> </tr> </thead> </table>	xi	3	4	5	6	7	8	fi	4	9	10	8	6	3																																					
xi	3	4	5	6	7	8																																															
fi	4	9	10	8	6	3																																															
	Ans.	<table border="1" style="margin: auto;"> <thead> <tr> <th>xi</th> <th>fi</th> <th>fi xi</th> <th>Di = xi - x̄ </th> <th>fi Di</th> </tr> </thead> <tbody> <tr> <td>3</td> <td>4</td> <td>12</td> <td>2.3</td> <td>9.2</td> </tr> <tr> <td>4</td> <td>9</td> <td>36</td> <td>1.3</td> <td>11.7</td> </tr> <tr> <td>5</td> <td>10</td> <td>50</td> <td>0.3</td> <td>3</td> </tr> <tr> <td>6</td> <td>8</td> <td>48</td> <td>0.7</td> <td>5.6</td> </tr> <tr> <td>7</td> <td>6</td> <td>42</td> <td>1.7</td> <td>10.2</td> </tr> <tr> <td>8</td> <td>3</td> <td>24</td> <td>2.7</td> <td>8.1</td> </tr> <tr> <td></td> <td>40</td> <td>212</td> <td></td> <td>47.8</td> </tr> </tbody> </table> $\bar{x} = \frac{\sum f_i x_i}{N} = \frac{212}{40} = 5.3$ $M.D. = \frac{\sum f_i D_i}{N}$ $= \frac{47.8}{40}$ $= 1.195$	xi	fi	fi xi	Di = xi - x̄	fi Di	3	4	12	2.3	9.2	4	9	36	1.3	11.7	5	10	50	0.3	3	6	8	48	0.7	5.6	7	6	42	1.7	10.2	8	3	24	2.7	8.1		40	212		47.8	<p>1+1</p> <p>1</p> <p>1/2</p> <p>1/2</p>	<p>4</p>									
xi	fi	fi xi	Di = xi - x̄	fi Di																																																	
3	4	12	2.3	9.2																																																	
4	9	36	1.3	11.7																																																	
5	10	50	0.3	3																																																	
6	8	48	0.7	5.6																																																	
7	6	42	1.7	10.2																																																	
8	3	24	2.7	8.1																																																	
	40	212		47.8																																																	